# Forecasting the Impact of Waste on Environmental Pollution

Asst.Lecturer Asraa S. Alwan College of Admin.& Eco, Sulaimani University. University. Email: <u>asraa.alwan@univsul.edu.iq</u>

Dr.Waleed Miyah Rodeen College of Admin&Eco, Basra University University. Email: waleed\_basrah@yahoo.com Asst.Lecturer Shaho T. College of Admin.& Eco, Sulaimani

Email:shaho.ahmed@univsul.edu.iq

Asst.Lecturer Hindreen A. Tahir College of Commerce, Sulaimani

Email: hindreen.taher@univsul.edu.iq

## Abstract

Reducing pollution of environment is an important aim of this study, Box-Jenkins models cannot predict volatility even if its residuals having ARCH effect, the GARCH (1,1) model have been used because the residuals of the mean equation has ARCH effect. Depending on GARCH (1,1) model we forecasted for sixty days respectively, the forecasted weight of waste is increasing it implies that the pollution of environment is also increased if the waste does not disposed of in a scientific way.

Key word: Time series analysis, Box-jenkins method, ARCH and GARCH method.

## التنبؤ بتاثير كمية النفايات على تلوث البيئة

مقدم من

هندرین عبداللہ طاہر	د.وليد ميه رودين	شاهو طاهر احمد	اسراء سعدون علوان
مدرس مساعد	مدرس	مدرس مساعد	مدرس مساعد
كلية التجارة	كلية الادارةوالاقتصاد	كلية الادارةوالاقتصاد	كلية الادارةوالاقتصاد
جامعة السليمانية	جامعةالبصرة	جامعة السليمانية	جامعة السليمانية

#### المستخلص

ان الهدف من هذه الدراسة هو النتبؤ بتاثير كمية النفايات على تلوث البيئة,وعند دراسة هذا الموضوع كان لا بد من استخدام انموذج احصائي ياخذ بنظر الاعتبار التقلبات التي تحدث في كميات النفايات

حيث ان النفايات هي مجمل مخلفات الأنشطة الإنسانية المنزلية والزراعية والصناعية والإنتاجية، أي كل المنقولات المتروكة أو المتخلى عنها في مكان ما ، والتي ترْكُها يهدد ويسيء إلى الصحة و السلامة العامة.

تم استخدام بيانات من الشركة الوطنية للتنظيف في محافظة البصرة في العراق وهي ثالث محافظة تحتوي على الاهوار وشط العرب وهي المنفذ المائي الى الخليج العربي

وان ادارة النفايات تعتمد على الاليات المستخدمةلنقل النفايات يوميا وعدد العمال المستخدمين في كل يوم كما ان عدد النفايات اليومية يعد امرا مهما اضافة الى وزن النقلة الواحدة

تم اخذ هذي المتغيرات بشكل يومي ولمدة 5سنوات يعني 1825يوم وحيث ان هناك تقلب في السلسة الزمنية ولمعالجة هذه المشكلة قدم الباحث Engle في عام 1982 نموذج ال ARCH وفي عام 1986 اضافة العالم Bollersley حدود الانحدار الذاتي ليتحول الى نموذج غارش يتم اختبار هذا النموذج ومعرفة فيما اذا يحقق الشروط او الكفائة الخاصة به حيث قمنا باستخدام برنامج Eviewلحساب المقدرات الاحصائية والاستنتاج بان اسلوب غارش افضل من الاساليب السابقة وكمية النفايات في زيادة مستمرة نوصي لحل هذا الموضوع باستخدام اساليب علمية للتخلص من النفايات واعادة التدوير ,استخدام اسلوب التوعية الصحية للمواطنين....لان التخلص من النفايات ليست مسؤولية الحكومة بحد ذاتها وانما هي مسؤولية مشتركة بين المواطن والحكومات ,عقد ندوات لطلاب الجامعات لزيادة الوعي الثقافي

### **1-1 Introduction**

There are several definitions of the term waste. The Solid wastes include substances originating from both human and animal activities, usually disposed it because they are no longer required and these useless materials (solid waste) consist of industrial, non-industrial and domestic hazardous waste. For Examples of these solid waste are household organic rubbish, institutional rubbish, construction waste, and street surveys. The World Health Organization (WHO) has defined waste as some of the things that its owner does not want it, and which haven't any benefit, English law defines it as any material resulting from any production process, or any material, equipment, broken, damaged, idle, contaminated material or any excess clothing.

#### **1-2 Type of Waste**

- 1. Hazardous solid waste: Waste from different processes that retain the properties of a hazardous substance that does not have alternative uses. It is a source of danger to human health and the elements of the environment because it contains toxic or explosive materials. The sources of these wastes include industrial and agricultural sources, hospitals and health facilities. And pharmaceuticals
- Non-hazardous solid waste: solid waste that does not contain substances or components that have the characteristics of hazardous substances, and they vary in their chemical and physical properties and include organic and inorganic substances such as:
  - a. Municipal waste: waste produced from the kitchens of houses, shops, markets, and restaurants through the preparation, cooking and serving of

food. It is mainly composed of organic substances that can be rotted and damp, and contains free liquids in small quantities

- b.Industrial waste: There are many industrial activities in the countries, resulting in waste such as industrial waste. The quality and quantity of industrial solid waste vary according to the quality of the industry and the method of production.
- c. Agricultural Waste: Agricultural waste includes all waste or waste resulting animal, and slaughterhouse activities. The most from all agricultural, important of these wastes are animal secretions, fodder residues and plant harvesting waste. In general, these agricultural wastes are not an environmental problem if they are returned to normal
- d.Health waste and laboratories are all solid, liquid and gaseous wastes that include sharp teeth, blood, body organs, chemicals, drugs, pharmaceuticals, medical instruments and radioactive materials from various health care institutions, medical laboratories, medical research centers, pharmaceutical factories and warehouses, hospitals and medical clinics.

#### **1-3Factors influencing waste increase**

- The number of population: directly proportional to the amount of waste as the number of individuals increased the amount of waste produced by each individual and in the countryside where the waste generated in cities and urban areas are usually higher than in rural areas.
- Industrial development: The increase in factories contributed to the provision of canned food, ready-made cups, spoons and plastic and paper dishes are not usable again made them a cause of accumulation of household waste.
- Economic development: The waste generated by the economic level of the country and the rapid urbanization and income levels of the population, which are the main factors in the waste disposal process, are affected.
- 4. Social conditions: Adhering to tribal customs and traditions by providing large quantities of food and beverages during the occasions, holidays and orphanages

and the absence of canned foods, which results in increasing the volume of household waste, especially organic ones.

5. Climate conditions: The quantity of waste and the quality of waste generated vary according to the four seasons.

#### 1-4 Waste management

The waste management principle is based on thinking not only on the disposal of waste, but also on finding solutions and ways of handling the huge amounts generated each day. Waste management has a set of foundations for applying this principle, including:

- 1. Reduce the use of raw materials.
- 2. Reuse of some solid waste components.
- 3. Extraction of energy from solid waste.
- 4. Recycling some solid waste elements.
- 5. Final disposal process.
- 6. Daily waste management.

## **Chapter Two**

#### Methodology

### 2-1 Building a GARCH Model<sup>[1]</sup>

For building any ARCH or GARCH model in time series analysis the below steps are required:

1. Construct an appropriate first moment model using either an ARIMA, regression, or transfer function model, and use the residual series  $(a_i^{\wedge})$  of the model to exam for the presence of GARCH effects.

- 2. Explain an appropriate GARCH model for  $a_t^2$  and perform parameter estimation;
- 3. Study the fitted GARCH model and refine it if necessary.

#### 2-2 Testing GARCH Effects (Test of heteroscedasticity)<sup>[6][4][2]</sup>

The availability of ARCH/GARCH effects may give serious model miss-specification if they are ignored. Logically ignoring ARCH effects will give the identification of ARMA models that are over-parameterized. In addition, as with all forms of heteroscedasticity,

Estimation assuming its absence will result in inappropriate standard errors of parameter estimates which are typically smaller than what they should be. Therefore it is important to check the presence of GARCH effects in time series modeling.

Two ways of testing GARCH effects are used. Number one is to check the Ljung-Box portmanteau Q statistics of  $a_t^2$ . McLeod and Li show that the sample autocorrelations of  $a_t^2$  have asymptotic variance  $n^{-1}$  and that portmanteau statistics calculated from them are asymptotically  $\chi^2$  if the  $a_t^2$  are independent. Since the sample autocorrelations of  $a_t^2$  are also useful for the identification of an GARCH model for  $a_t^2$ .

Number two checking conditional heteroscedasticity is to use the Lagrange multiplier test of Engle. Consider the following regression model for

$$a_t^2 \operatorname{on} a_{t-j}^2$$
 j=1,2,....m  
 $a_t^2 = \alpha_0 + \alpha_1 a_{t-1}^2 + \alpha_2 a_{t-2}^2 + \dots + \alpha_m a_{t-m}^2 + v_t$  t=m+1.....n (2-1)

Where vt denotes the error term, m is a pre-specified positive integer, and n is the total number of observations in the series. Using  $R^2$  to denote the *coefficient of determination* from (2.1), Engle shows that under the null

hypothesis  $H_0: \alpha_1 = \alpha_2 = \dots \alpha_m = 0$ ,  $nR^2$  asymptotically follows  $a\chi^2$  -distribution with m degrees of freedom.

## **2-3** Normal Distribution <sup>[3]</sup>

Taking that  $a_t^2$  follows a GARCH (1, 1) model and  $\varepsilon_t$  follows a Normal

distribution, the maximum likelihood estimates of the GARCH(1,1) model for series are.

$$y_{t} = c_{1} + a_{t}$$
  
 $\sigma_{t}^{2} = c_{2} + GMA \ a_{t-1}^{2} + GAR \ \sigma_{t-1}^{2}$ 

## 2-4 Volatility

Volatility is an important factor in options trading. Here volatility means the conditionalvariance of the underlying asset return.

## 2-5 Identification of a GARCH Model<sup>[3]</sup>

If the Ljung-Box statistics and LaGrange multiplier (LM) test are significant, then conditional heteroscedasticity of  $a_t^2$  is present, and we need to identify an appropriate GARCH model for  $a_t^2$ . However since the GARCH (1,1) model has been shown to be appropriate in many empirical studies, we may employ the GARCH(1,1) model at the beginning of the analysis. As the model is estimated, diagnostic checking procedures may be followed to see if the GARCH (1,1) model is okay, or if the orders of the GARCH model should be increased or

decreased. Instead of using this trial-and-error approach, we may use the following procedure for the definition of a GARCH model for the  $\{a_t^2\}$  series.

# 2-6 Ljung-Box Q-Statistic <sup>[1] [5] [4]</sup>

Adding to the visual inspection of the plotted autocorrelation, the Ljung-Box Q-Statistic is Used for diagnostic checking .The Ljung-Box Q-Statistic is defined by equation (2-2)

$$Q^* = n(n+2)\sum_{j=1}^{K} (n-j)^{-1} r_j^2(e_t)$$
(2-2)

Where n is the number of observation, K is the largest lag used and rj is the sample autocorrelation function at lag j of an appropriate time series  $a_t$ , for example.

Statistic  $r_j$  for  $a_i$  is then defined as

$$r_{j} = \frac{\sum_{t=j+1}^{n} (a_{t} - a)(a_{t-j} - a)}{\sum_{t=1}^{n} (a_{t} - a)^{2}}$$
(2-3)

The Q-Statistic is a modification of the Box-Pierce test statistic, this was suggested for testing ARIMA and ARMA models both the test statistics are determined by the calculation of the sample autocorrelation function for the residuals  $\varepsilon_t^{\uparrow}$  from those models .the similar test statistic based on different calculation using the autocorrelation function will be high benefit for small sample applicability, it is defined as

$$Q^* = n(n+2) \sum_{j=1}^{K} \frac{r_j^2(e_j)}{(n-j)} \sim \chi_k^2$$
(2-4)

And  $r_j^*$  is

$$r_{j}^{*} = \sum_{t=j+1}^{n} (a_{t}^{2} - a) (a_{t-j}^{2} - a) / \sum_{t=1}^{n} (a_{t}^{2} - a)$$
(2-5)

# 2.7 Likelihood Function of GARCH Models <sup>[3] [5]</sup>

By defining  $\alpha = [\alpha_0, \alpha_1, \dots, \alpha_m, B_1, \dots, B_r, \eta]'$ , the log likelihood functions of  $\alpha$  may be derived Under the Normality assumption of  $\varepsilon_t$ . If  $\varepsilon_t$  is assumed to follow a Normal distribution. However, practically, there

is substantial evidence showing that this assumption may not all the time be satisfactory.

For the GARCH (1.1) model, the joint density of the observations  $a_1, \dots, a_T$  can be calculated as the product of the conditional densities, conditioning on the last observations

$$fa_1, \dots, a_T(a_1, \dots, a_T) = \{\prod_{i=2}^T fa_i | a_1, \dots, a_{i-1}(a_i) | a_1, \dots, a_{i-1}(a_i) \} * fa_1(a_1)$$
(2-6)

Easy way, the marginal density of  $a_1$  will be dropped as for ARIMA (1.1) model. For k=2,...T the conditional density of  $a_k$ , conditioning on  $a_1$ ..... $a_{k-1}$  is

$$fa_{k} | a_{1}, \dots, a_{k-1}(a_{k} | a_{1}, \dots, a_{k-1}) = \frac{1}{\sqrt{2\pi} \sqrt{\sigma_{k}^{2}}} \exp\left\{-\frac{a_{k}^{2}}{2\sigma_{k}^{2}}\right\}.$$
 (2-7)

And the conditional likelihood function given  $a_i$  and  $\sigma_i^2$  is :

$$L(\alpha_{0}, \alpha_{1}, B_{1}) = fa_{2}, \dots a_{T} \left| a_{1} \sigma_{1}^{2} (a_{2}, \dots a_{T} \left| a_{1} \sigma_{1}^{2} \right) \right|$$

$$\prod_{i=2}^{T} \frac{1}{\sqrt{2\pi} \sqrt{\sigma_{i}^{*2}}} \exp\left\{ -\frac{a_{i}^{2}}{2\sigma_{i}^{*2}} \right\}.$$
(2-8)

Where  $\sigma_i^{*2} = \alpha_0 + \alpha_1 a_{i-1}^2 + B_1$  are obtained recursively. We substitute  $\sigma_i^2$  by its expected value  $E(\sigma_i^2) = \frac{\alpha_0}{1 - \alpha_1 - B_1}$  (2-9)

Using the logarithm and ignoring the constant term we find that the log likelihood function is:

$$l(\alpha_0, \alpha_1, B_1 | a, \sigma^2) = -\frac{1}{2} \left\{ \sum_{i=2}^T \log \sigma_i^{*2} + \frac{a_i^2}{\sigma_i^{*2}} \right\}$$
(2-10)

Where  $a = (a_1, ..., a_T)^{-1}$  and  $\sigma_t^2 = (\sigma_1^2, ..., \sigma_T^2)$ .

## 2-8 Model Checking of GARCH (r,m)<sup>[3]</sup>

For a GARCH model, the standardized shocks  $\varepsilon_i^{\wedge} = a_i^{\wedge} / \sigma_i^{\wedge}$  are *i.i.d.* random errors following either a standard Normal or a non-Normal distribution such as the standardized Student-t distribution. Therefore, one can check the adequacy of a fitted GARCH model by examining the series {  $\varepsilon_i^{\wedge}$  }. In particular, the sample autocorrelations and the Ljung-Box Q statistics of  $\varepsilon_i^{\wedge}$  can be used to check the adequacy of the mean (first moment) equation and those of  $\varepsilon_i^2$  can be used to test the validity of the volatility (second moment) equation.

## 2-9 Existence of the GARCH (1,1) process<sup>[5]</sup>

The GARCH(1,1) model is:

$$a_{t} \sim N(0, \sigma_{t}^{2})$$

$$\sigma_{t}^{2} = \alpha_{0} + \alpha_{1}a_{t-1}^{2} + B_{1}\sigma_{t-1}^{2}$$
(2-11)

Where  $\alpha_0 > 0$ ,  $\alpha_1 \ge 0$  and  $B_1 \ge 0$ .

GARCH (r,m) processes are defined recursively and conditions are needed to guarantee the existence of stationary solutions. Now we derive such conditions for the GARCH (1,1) process Dividing by the square root of the conditional variance of  $a_t$  from (2-11). We got  $\varepsilon_t \sim N(0,1)$ 

$$\sigma_t^2 = \alpha_0 + \alpha_0 \sum_{k=1}^{\infty} \left( \prod_{j=1}^k (\alpha_1 E(a_{t-j}^2 + B_1)) \right)$$
(2-12)

**Theorem 2-1**<sup>[5]</sup>: if the expectation of an infinite sum of non-negative random variables is finite, then the sum converges almost surely.

(see Lucas 1975, theorem 4,2,1, p. 80.)

We will use this theorem to find a condition under which the equations in (2-12) exists. Using the unconditional expectation of both sides, resulting in

$$E(\sigma_{t}^{2}) = \alpha_{0} + \alpha_{0} \sum_{k=1}^{\infty} (\prod_{j=1}^{k} (\alpha_{1} E(a_{t-j}^{2} + B_{1})))$$
  
$$= \alpha_{0} + \alpha_{0} \sum_{k=1}^{\infty} (\alpha_{1} + B_{1})^{k}$$
  
$$= \frac{\alpha_{0}}{1 - \alpha_{1} - B_{1}}$$
(2-13)

So the unconditional expected value of  $\sigma_t^2$ , is the finite and the infinite series for  $\sigma_t^2$  in (2-12) converges to  $\alpha_0/(1-\alpha_1-B_1)$  provided that  $\alpha_1 + B_1 < 1$ . In summary, if  $\alpha_1 + B_1 < 1$  and  $\alpha_1 \ge 0$ ,  $B_1 \ge 0$ , we can define  $\sigma_t^2$  by (2-12) and  $a_t = \varepsilon_t \sqrt{\sigma_t^2}$  the resulting process {  $a_t$  } is a stationary solution of (2-11).

# 2-10 Forecasting GARCH (1,1) Model<sup>[3]</sup>

Forecasts of a GARCH model can be found by using methods similar to those of an ARMA model. Consider the GARCH (1, 1) model in assume that the forecast origin is n. For one-step-ahead forecast, we have

$$\sigma_{n+1}^{2} = \alpha_{0} + \alpha_{1}a_{n}^{2} + B_{1}\sigma_{n}^{2}$$
(2-14)

Where  $a_n^2$  and  $\sigma_n^2$  are known at t=n .therefore, the one- step ahead forecast is

$$\sigma_n^2(1) = \alpha_0 + \alpha_1 a_n^2 + B_1 \sigma_n^2$$
(2-15)

For multi-step ahead forecasts, we use  $a_t^2 = \sigma_t^2 \varepsilon_t^2$ 

$$\sigma_{t+1}^{2} = \alpha_{0} + (\alpha_{1} + B_{1})\sigma_{t}^{2} + \alpha_{1}\sigma_{t}^{2}(\varepsilon_{t}^{2} - 1)$$
(2-16)

When t=n+1, the equation becomes

$$\sigma_{n+2}^{2} = \alpha_{0} + (\alpha_{1} + B_{1})\sigma_{n+1}^{2} + \alpha_{1}\sigma_{n+1}^{2}(\varepsilon_{n+1}^{2} - 1)$$
(2-17)

since  $E(\varepsilon_{n+1} - 1 | F_n) = 0$ , the two –step ahead volatility forecast at the forecast origin n satisfies the equation

$$\sigma_n^2(2) = \alpha_0 + (\alpha_1 + B_1)\sigma_n^2(1)$$
(2-18)

In general, we have

$$\sigma_n^2(\ell) = \alpha_0 + (\alpha_1 + B_1)\sigma_n^2(\ell - 1) , \quad \ell > 1$$
 (2-19)

This result is exactly the same as that of an ARMA (1, 1) model with an AR polynomial 1– ( $\alpha_1 + B_1$ ) B. By repeated substitutions in (2-19),

the  $\ell$  -step-ahead forecast can be written as

$$\sigma_n^2(\ell) = \frac{\alpha_0 [1 - (\alpha_1 + B_1)^{\ell-1}]}{1 - \alpha_1 - B_1} + (\alpha_1 + B_1)^{\ell-1} \sigma_n^2(1)$$
(2-20)

Therefore:

$$\sigma_n^2(\ell) \to \frac{\alpha_0}{1 - \alpha_1 - B_1} = \alpha_0^*, \quad as \quad \ell \to \infty$$
(2-21)

Provided that  $\alpha_1 + B_1 < 1$ 

Consequently, the multi-step-ahead volatility forecasts of a GARCH (1, 1)model converge to the unconditional variance of  $a_r$  as the forecast horizon increases to infinity provided that Var ( $a_r$ ) exists.

# **Chapter Three**

## Applications

## 3-1 Fitting mean equation model

The series of the study should be stationary, therefore the ADF test of the stationarity have been used as it is shown below in table (1):

		t-Statistic	Prob.*
Augmented Dickey-Ful Test critical values:	ller test statistic 1% level	-6.762935 -3.449797	0.0000
	5% level 10% level	-2.870004 -2.571349	

Tabl	le (	1)	Represents	the stationarity	test results.
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From the above table it is obviouse that the p-value is less than 0.05 that mean the series is stationary



Figure (1) Represents the graph of the series

After achiving the stationarity condition of the series we should fit mean equation model as it is shown below:

Table (2) Represents the fit of mean equation model

Dependent Variable: ZT Method: Least Squares Date: 08/18/17 Time: 17:23 Sample: 1 335 Included observations: 335									
Variable Coefficient Std. Error t-Statistic Prob.									
С	2.911045	0.022659	128.4703	0.0000					

Frome table (2) the p-value is less than 0.05 then one can say that the model is significant.



Figure(2) Represents the residuals of the mean equation

The hypothesis of ARCH has effect or not on the mean equation for this purpose heteroskedasticity test ARCH have been used and its results are shown in table (3):

H<sub>0</sub>: There is no ARCH effect Vs H1: there is ARCH effect

Table (3) Represents the heteroskedasticity test ARCH

Heteroskedasticity Test: ARCH							
F-statistic	13.415662	Prob. F(1,332)	0.003				

The P-value is less than 0.05 then the null hypothesis should be rejected, in another word there exist ARCH effect.

We achived two main assumptions of using GARCH model which are the stationary of the series and effect of ARCH in the mean equation mmodel then GARCH model can be used to forecat the volatility.

## 3-2 Fitting GARCH (1,1)

The GARCH (1,1) model have been runned, the results of its fit is shiown in table (4) below:

Variable	Coefficient	Std. Error	z-Statistic	Prob.			
С	2.836153	0.018968	149.5258	0.0000			
Variance Equation							
C RESID(-1)^2 GARCH(-1)	0.018268 0.229532 0.649460	0.008899 0.102049 0.127342	2.052893 2.249229 5.100128	0.0401 0.0245 0.0000			

Table (4) Represents the fit of GARCH (1,1) model

From the above table it is obviouse that the estimators of the variance equation are significant depending the p-value which is less than 0.05.

The residuals of the GARCH (1,1) model should be tested in order to find out that the model is suffer from serial correlation of residuals or not

 $H_0$ : There is no serial correlation of residuals. Vs  $H_1$ : There is serial correlation of residuals.

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob*
. <b>d</b> .	1 101	1	-0.025	-0.025	0.2058	0.650
ı 🚺 i	j uju	İ 2	-0.020	-0.020	0.3394	0.844
ı 🗍 i	j uju	3	-0.021	-0.022	0.4837	0.922
. i∎i	i(i	4	-0.012	-0.014	0.5331	0.970
ul i	iti	5	-0.013	-0.014	0.5893	0.988
i 🌓	i <b>l</b> i	6	-0.020	-0.022	0.7303	0.994
i 🌓	i <b>l</b> i	7	-0.019	-0.021	0.8484	0.997
i 🌓	ı <b>l</b>  ı	8	-0.024	-0.027	1.0469	0.998
ı 🖡 i	i <b>l</b> i	9	-0.007	-0.010	1.0630	0.999
. I∎I	i <b>(</b> i	10	-0.008	-0.011	1.0856	1.000
u¶u	i¶i	11	-0.019	-0.022	1.2124	1.000
. ∎i	III	12	0.026	0.022	1.4500	1.000
111	( <b> </b> )	13	0.007	0.005	1.4654	1.000
. I∎ I	i¶i	14	-0.014	-0.015	1.5320	1.000
. I∎ I	ı <b>l</b> ı	15	-0.023	-0.025	1.7189	1.000
. I¶ I	i <b>l</b> i	16	-0.009	-0.012	1.7471	1.000
. I∎ I	l di	17	-0.017	-0.020	1.8482	1.000
I I I	I <b> </b> I	18	-0.002	-0.006	1.8502	1.000
. I∎ I	i¶i	19	-0.012	-0.014	1.8978	1.000
u <b>ļ</b> u	i¶i	20	-0.016	-0.019	1.9888	1.000
ı <b>≬</b> ı	ļ iļi	21	0.035	0.031	2.4220	1.000
ı <b>≬</b> ı	i <b>(</b> i	22	-0.015	-0.018	2.5038	1.000
ı <b>≬</b> ı	i <b>(</b> i	23	-0.011	-0.014	2.5493	1.000
ı <b>≬</b> ı	ı <b>(</b>	24	-0.024	-0.028	2.7659	1.000
. I∎I	i <b>(</b> i	25	-0.004	-0.010	2.7727	1.000
ı <b>≬</b> ı	i <b>(</b> i	26	-0.009	-0.014	2.8046	1.000
. I∎I	I <b> </b> I	27	0.005	0.003	2.8154	1.000
ı <b>D</b> i	ļ iļu	28	0.050	0.047	3.7167	1.000
I.∎I	I <b> </b> I	29	0.004	0.005	3.7216	1.000
i 🌓	i <b>l</b> i	30	-0.021	-0.022	3.8807	1.000
i 🌓	i <b>l</b> i	31	-0.012	-0.014	3.9308	1.000
ı <b>İ</b> I	ļ i <b>ļ</b> i	32	-0.003	-0.004	3.9336	1.000
i 🌓	i <b>l</b> i	33	-0.010	-0.015	3.9701	1.000
i 🌓	i <b>l</b> i	34	-0.009	-0.011	3.9989	1.000
i 🌓	i¶i	35	-0.018	-0.019	4.1151	1.000
i <b>≬</b> i	i <b>ļ</b> i	36	-0.006	-0.006	4.1289	1.000

Table (5) Represents testing of ACF and PACF

From the above table the p-value for the 36 laggs are greater than 0.05 then we can accept the null hypothesis.

The final test is heteroskedasticity test:ARCH to figure out that the postulated model is adequate or not, the results is shown in table (6) below:

 $H_0$ : ARCH has no effect. Vs  $H_1$ : ARCH has effect.

Table (6) Represents the test of ARCH effect.

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F-statistic	0.093045	Prob. F(1,332)	0.7605
Obs*R-squared	0.093580	Prob. Chi-Square(1)	0.7597

From the above table it is clear that the P-value is greater than 0.05 then we can  $% \left( H_{0}\right) =0.05$  accept  $H_{0}$  .



Figure (3) Represents the graph of actual, forecasted and residuals.

Laggs	Forecasted	Laggs	Forecasted	Laggs	Forecasted
336	2.8	356	2.83	376	2.7
337	3.1	357	2.43	377	2.9
338	3.2	358	3.03	378	2.7
339	3.3	359	2.43	379	2.6
340	3	360	2.93	380	2.7
341	3	361	2.43	381	2.8
342	3	362	2.93	382	2.8
343	2.7	363	2.33	383	2.9
344	3	364	2.53	384	2.8
345	3.1	365	2.73	385	3
346	3.1	366	3.1	386	3.1
347	3.1	367	3.8	387	3.3

Table (7) Represents the forecasted values

348	2.6	368	3.9	388	3.3
349	2.8	369	3.1	389	2.9
350	2.7	370	3.1	390	2.8
351	2.53	371	3.1	391	2.8
352	2.43	372	3.3	392	3.1
353	2.43	373	3.6	393	3.3
354	2.33	374	2.7	394	3.3
355	2.53	375	2.9	395	3.1

## **4-1 Conclusions**

- 1- GARCH model is more adequate for the series that its residuals are affected by ARCH.
- 2- Any time series models after fitting its residuals should be tested to figure out that there exist any pattern in the residuals or not.
- 3- GARCH models provides the forecasting for volatility for each observation.

## **4-2 Recommendations**

In this paper according to forecasted values there exist an increasing of the weight of waste which implies that the environment will be in danger, therefor the stack holders must warring citizens through posters, T.V programs and seminars at the colleges to raised people awareness towards pollution of environment.

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